ARTICLE

Open Access

Broadband and fabrication-tolerant 3-dB couplers with topological valley edge modes

Guo-Jing Tang¹, Xiao-Dong Chen[™], Lu Sun², Chao-Heng Guo¹, Meng-Yu Li¹, Zhong-Tao Tian¹, Hou-Hong Chen¹, Hong-Wei Wang², Qi-Yao Sun², Ying-Di Pan², Xin-Tao He[™], Yi-Kai Su[™] and Jian-Wen Dong[™]

Abstract

3-dB couplers, which are commonly used in photonic integrated circuits for on-chip information processing, precision measurement, and quantum computing, face challenges in achieving robust performance due to their limited 3-dB bandwidths and sensitivity to fabrication errors. To address this, we introduce topological physics to nanophotonics, developing a framework for topological 3-dB couplers. These couplers exhibit broad working wavelength range and robustness against fabrication dimensional errors. By leveraging valley-Hall topology and mirror symmetry, the photonic-crystal-slab couplers achieve ideal 3-dB splitting characterized by a wavelength-insensitive scattering matrix. Tolerance analysis confirms the superiority on broad bandwidth of 48 nm and robust splitting against dimensional errors of 20 nm. We further propose a topological interferometer for on-chip distance measurement, which also exhibits robustness against dimensional errors. This extension of topological principles to the fields of interferometers, may open up new possibilities for constructing robust wavelength division multiplexing, temperature-drift-insensitive sensing, and optical coherence tomography applications.

Introduction

Photonic integrated circuits provide an efficient platform for optical interconnection^{1,2}, optical sensing³, integrated quantum circuits⁴ and optical neural networks⁵, and find broad applications in high-speed communication, internet of things, quantum information technology and artificial intelligence. Among the fundamental components in these circuits is the 3-dB coupler, which facilitates the equal splitting of signal power for onchip information processing. Conventional 3-dB couplers, such as directional couplers (DCs), face challenges of limited operation bandwidth and weak robustness because the power partition is governed by the interference of two modes in coupled waveguides^{6,7}. Consequently, the splitting ratio has serious sensitivity to working wavelength and fabrication dimensional errors.

Yi-Kai Su (yikaisu@sjtu.edu.cn) or Jian-Wen Dong (dongjwen@mail.sysu.edu.cn) ¹School of Physics & State Key Laboratory of Optoelectronic Materials and Technologies, Sun Yat-sen University, Guangzhou 510275, China ²State Key Laboratory of Advanced Optical Communication Systems and Networks, Department of Electronic Engineering, Shanghai Jiao Tong University, Shanghai 200240, China

These authors contributed equally: Guo-Jing Tang, Xiao-Dong Chen, Lu Sun

To mitigate these issues, researchers have proposed and implemented various well-designed nano-structures^{8–17}, including adiabatic evolution structures, asymmetric waveguides, multiple sections and sub-wavelength structures. While the performance of the optimized 3-dB couplers is improved, the splitting ratios are still wavelength dependent due to the reliance of interference principles. To overcome such limitation, it is necessary to explore new physical principles beyond interference so as to achieve a broadband and fabrication-tolerant 3-dB coupler.

Topological nanophotonics, a recently flourishing research field that combines the topological physics with nanophotonics^{18–26}, offers exciting opportunities for realizing robust waveguides^{27–36}, on-chip micro-cavities^{37–43} and advanced lasers^{44–50}. As one of representative topological nanostructures, valley photonic crystals (VPCs) support edge modes with inter-valley-scattering suppression⁵¹. These valley edge modes are resilient against perturbations that do not mix the two valleys. It should be emphasized that VPCs cannot completely eliminate radiation losses resulting from arbitrary perturbations, which is predicted by an early theoretical

© The Author(s) 2024

Open Access This article is licensed under a Creative Commons Attribution 4.0 International License, which permits use, sharing, adaptation, distribution and reproduction in any medium or format, as long as you give appropriate credit to the original author(s) and the source, provide a link to the Creative Commons licence, and indicate if changes were made. The images or other third party material in this article are included in the article's Creative Commons licence, unless indicated otherwise in a credit line to the material. If material is not included in the article's Creative Commons licence and your intended use is not permitted by statutory regulation or exceeds the permitted use, you will need to obtain permission directly from the copyright holder. To view a copy of this licence, visit http://creativecommons.org/licenses/by/4.0/.

Correspondence: Xin-Tao He (hext9@mail.sysu.edu.cn) or

study¹⁸ and further confirmed through a recent experimental demonstration⁵². VPCs have found applications in various areas, with one notable example being the realization of broadband robust transport through sharp-bent waveguides, as well as the demonstration on the subsequent splitting phenomena^{53–55}. Therefore, VPCs hold great promise for achieving wavelength-independent splitting, addressing the issues associated with operation bandwidth and fabrication tolerance.

In this work, we utilize VPCs to develop a topological 3-dB coupler. We thoroughly investigate the operational principles of such topological couplers and discover a scattering matrix insensitive to wavelength, resulting in the ideal 3-dB power splitting. This broadband and robust splitting ratio is achieved through the combination of valley-Hall topology and mirror symmetry. The 3-dB power splitting supports a wide wavelength range around 1550 nm and exhibits tolerance to dimensional errors, as compared to the case of conventional DCs. To further demonstrate its functionality, we propose an on-chip Michelson-like interferometer by utilizing the aforementioned topological coupler. We experimentally validate its capability of extracting length differences and demonstrate its robustness against dimensional errors. These findings highlight the resilience of the splitting ratio and the potential of realizing broadband and fabricationtolerant topological 3-dB couplers in a wide variety of applications such as sensing, information processing, and optical coherence tomography.

Results

Design of 3-dB couplers with topological valley edge modes

Consider a conventional 3-dB coupler, such as DC, consists of four ports [labeled with 1-4 in Fig. 1a]. Its performance is described by a 4×4 scattering matrix $S = (s_{mn})_{4 \times 4}$, where s_{mn} represents the field intensity ratio between the output port m and the input port n. At the wavelength of λ_1 , the ideal 3-dB power splitting occurs, dividing the input signal from port 1 into two signals of equal powers at the port 3 and port 4, i.e., $|s_{31}|^2 = |s_{41}|^2$. However, this 3-dB splitting is achieved at a single wavelength due to the interference between waveguide modes. Any fabrication dimensional errors or changes in working temperature would degrade the 3-dB splitting at the designed wavelength, significantly hindering the device performance. To overcome these limitations and achieve a high-performance 3-dB coupler with wavelength-independent splitting ratio over a wide bandwidth, we incorporate topological principles into the design of nanophotonic devices. As illustrated in Fig. 1b, we have designed a topological 3-dB coupler based on the VPC slab, implemented on the silicon-on-insulator platform. Sandwiched between the silica substrate and the



cladding, the VPC slab is constructed by a honeycomb lattice of equilateral triangular holes with a lattice constant of a = 440 nm in a 220 nm-thick silicon layer. To create a nontrivial band gap capable of supporting transverse-electric-like edge modes, we set the side lengths of two holes, denoted as s_1 and s_2 , to different values (Fig. 1c). We choose the parameters of VPCs

according to the photonic band structures [see details in Supplementary Section G]. For VPC1, we set $s_1 = 0.4a$ and $s_2 = 0.7a$, while for VPC2, we set $s_1 = 0.7a$ and $s_2 = 0.4a$. It results in a common band gap spanning from 1486 nm to 1585 nm for both VPC1 and VPC2 [see details in Supplementary Section A]. Note that these two VPCs have distinct topological invariants, which are characterized by the valley Chern numbers with opposite signs, i.e. $C_{\nu} < 0$ for VPC1 and $C_{\nu} > 0$ for VPC2. Due to the bulkedge correspondence, the domain wall between VPC1 and VPC2 (Fig. 1c) can support valley-dependent edge modes, whose propagation direction $sgn[\nu_{q}]$ (the sign of group velocity) is equivalent to $\tau_z \text{sgn}[C_{\nu b}]$. Here $C_{\nu b}$ is the valley Chern number of VPC at the bottom of domain wall and $\tau_z = 1(\tau_z = -1)$ for K valley (K' valley). Edge21 supports rightward-propagating K valley and leftward-propagating K' valley edge modes, while Edge12 supports rightwardpropagating K' valley and leftward-propagating K valley edge modes. This valley contrasting edge modes suggests the suppression of the scattering between two valley edge modes.

Utilizing the two distinct edges, we design a topological coupler capable of achieving ideal 3-dB splitting. The device consists of a harpoon-shaped structure formed by connecting two different edges, resulting in four ports (Fig. 1b). To analyze its performance, we consider four cases when the light is incident from different ports. For example, when the light is incident from port 1, the rightward K valley edge mode along Edge21 is excited. Because of the inter-valley scattering suppression, both the leftward K' valley edge mode along Edge21 (backward to port 1) and the rightward K' valley edge mode along Edge12 (forward to port 2) are forbidden, indicated by two red crossings in Fig. 1b. This leads to $s_{11} = s_{21} = 0$, and consequently the incident light can only propagate to port 3 or port 4. As the coupler has the mirror symmetry, the incident light should be equally divided into port 3 and port 4, i.e., $s_{31} = s_{41} = \sqrt{2}/2$. This is confirmed by the full wave simulation in Fig. 1d. When light is incident from port 1, the simulated H_z field shows that the incident waves is equally divided and propagates along both the upper and lower channels, resulting the 3-dB splitting ratio between port 3 and port 4. Likewise, we determine the other elements of the scattering matrix and ultimately obtain the scattering matrix of the proposed topological coupler:

$$S = \frac{\sqrt{2}}{2} \begin{pmatrix} 0 & 0 & 1 & 1\\ 0 & 0 & 1 & -1\\ 1 & 1 & 0 & 0\\ 1 & -1 & 0 & 0 \end{pmatrix}$$
(1)

The derivation of each element of the scattering matrix is detailed in Supplementary Section C.

We note that the scattering matrix described above represents the ideal 3-dB splitting over a broad bandwidth that determined by the operation range of valley edge modes. The scattering matrix is derived from topology and symmetry, which are independent to wavelength and are always valid in the range of topological edge modes in band gap. Since no additional wavelength condition is required. the matrix elements are wavelengthindependent in this range. Therefore, the 3-dB splitting can be achieved in the operation range of edge modes. This remarkable characteristic is protected by the nontrivial valley-Hall topology and the mirror symmetry of the structure.

Experimental characterization of splitting ratio and robustness of topological 3-dB coupler

In this section, we present the experimental investigation of the topological 3-dB coupler. The topological couplers are fabricated on the SOI platform using a topdown nanofabrication process [see Methods for fabrication details]. The optical microscope image of the whole sample, including topological coupler, strip waveguides and grating couplers, is shown in Fig. 2a. For the convenience of measurement, the grating couplers of port 1 and port 2 are placed on the left side, and the couplers of port 3 and port 4 are placed on the right side. Figure 2b gives the scanning electron microscope (SEM) images of the splitting junction formed by VPC1 and the VPC2. The junction is constructed by four edges, of which three of them are Edge21 and one is Edge12.

To confirm the broadband and robust 3-dB splitting performance in experiment, a fiber-to-waveguide alignment system is set up to image the light energy output from the grating couplers and to measure the transmission spectra [see Methods for the optical measurement setup]. Figure 2c, d show the measured splitting ratio spectra for light input from four different ports. The splitting ratio in Fig. 2c is defined as the ratio of transmittances between port 3 and port 4 when the light is incident from port 1 (red line) or port 2 (blue line). The incident waves are equally divided at the junction and propagate along the upper and lower channels to the output ports, resulting in a near-3-dB splitting ratio between port 3 and port 4. Similarly, the splitting ratio of the transmittances between port 1 and port 2 is depicted in Fig. 2d, when the light is incident from port 3 (red line) or port 4 (blue line). The splitting ratio spectra remain flat and close to 3-dB within the topological band gap (from 1530 nm to 1583 nm) for all four cases, which is in good agreement with the simulation results [see details in Supplementary Section D]. Note that the experimental results are difficult to reach ideal 3-dB ratio, as the fabricated samples may have minor deviations from rigorous mirror symmetry and difference in coupling efficiency



between two output ports. We also show the far-field microscope images in Fig. 2e, f, with the light incident from port 1 and port 3 at a wavelength of 1550 nm, respectively. After splitting in the 3-dB coupler, the equally divided light is radiated into free space by grating couplers. In Fig. 2e, we observe strong and symmetric radiation patterns between the gratings of port 3 and port 4, while that of port 2 is comparatively low due to intervalley-scattering suppression. Similar results are observed in Fig. 2f when the light incident from port 3. However, the radiation patterns from port 1 and port 2 exhibit slight difference, primarily stemming from the varying insertion losses of port 1 and port 2.

During the processes of nanofabrication, fabrication errors are inevitable, including dimensional error, sidewall

roughness, defects and dislocations. Dimensional error is common for the fabrication of topological 3-dB coupler, corresponding to variations of ± 10 nm in the size of the VPC holes. Consequently, we demonstrate the tolerance analysis of topological 3-dB couplers against dimensional errors, which has practical significance for on-chip nanodevices. As shown in Fig. 3a, the side lengths of triangular holes are varied by Δs . Far-field microscope images show that the radiated patterns at $\lambda = 1550 \text{ nm}$ maintain symmetric profiles between the gratings of port 3 and port 4, even with ± 10 nm variations in the size of the VPC holes (Fig. 3a). Due to broadband operation of near 3-dB in topological coupler, the splitting ratio nearly remain as 3-dB in a wavelength range even the spectra shift. Originated from the broadband property, the experimental ratio spectra of these three cases (Fig. 3b) keep in a flat platform ranging from 1533 nm to 1581 nm (orange region), albeit with a blue shift as Δs increases. For comparison, we also consider the dimensional error of conventional DC, i.e. the gap width Δg between two coupled waveguides [see schematics in Fig. 3c]. For the cases of $\Delta g = \pm 10$ nm, the far-field microscope images have asymmetric radiated patterns between port 3 and port 4, although the case of $\Delta g = 0$ is symmetric. In contrast to the near 3-dB flat platform in topological coupler, the splitting ratio spectra of DC are oblique slopes, as shown in Fig. 3d. The 3-dB splitting of DC only occurs at a single wavelength which has a red shift as Δg increases. Consequently, the performance of conventional DC is strongly sensitive to the size variations, and this is unwanted when nanodevices with precise splitting ratio are required. Further to cascading several DCs, the sensitivity to wavelength and dimensional error will largely increase. In comparison, topological couplers still have flat splitting ratio even though they are cascaded under consideration of dimensional errors. It implicates topological coupler will exhibit better robustness in the cascaded devices of PICs, such as optical neural networks and quantum logic gates. Even though we introduce nonuniform dimensional errors which break the mirror symmetry, the splitting ratio still exhibits robustness as the structure of coupler and the dispersion of edge modes are not seriously changed. In addition to fabrication errors, temperature drift will variate the refractive index of semiconductor materials and thus affect the performance of 3-dB couplers. We show that topological couplers also outperform conventional couplers for the robustness against temperature changes. [see details in Supplementary Section D].

On-chip interferometer based on topological coupler

In addition to the demonstration of the principles of topological physics, another important goal in topological nanophotonics is to achieve robust optical functionality



even in the presence of fabrication errors. To verify this capability, we utilize the topological 3-dB coupler to construct an on-chip Michelson-like interferometer. The schematic in Fig. 4a illustrates the interferometer's configuration, which consists of a 3-dB coupler and a pair of distributed Bragg reflectors (DBRs) connected to the output waveguides of port 3 and port 4. The DBRs have reflectivity of over 90% from 1500 nm to 1600 nm. The magnified SEM image of the purple box in Fig. 4a shows the coupling area of port 1 (same to port 3 and port 4), where a $2 \mu m$ -width strip waveguide is connected to the VPC. The first 18 rows of VPC holes are modified to introduce adiabatic-like mode evolution, which would improve the coupling efficiency. For port 2 (see magenta box in Fig. 4a), a line-defect photonic crystal waveguide is introduced and connected to a 400 nm-wide strip waveguide.

This interferometer design can be used to carry out distance measurements. For example, in Fig. 4 the two output waveguides have a length difference of $100 \,\mu\text{m}$. The shorter one serves as the reference arm, while the longer one the measuring arm. In the experiment, the

light is input from port 1, split by the coupler, and directed to port 3 and port 4 [see red arrows]. The two coherent light beams are then reflected by DBRs, injected into port 3 and port 4, and interfere at the splitting junction of the coupler [see blue arrows]. The difference in waveguide lengths between the reference and measuring arms introduces a phase difference $\Delta \phi$, which determines the transmittance to port 2:

$$T_2(\lambda) = \frac{1}{2} [1 - \cos \Delta \phi(\lambda)]$$
⁽²⁾

Owing to the wavelength-dependent nature of the waveguide mode dispersion (i.e., $\Delta \phi$ is a function of wavelength), the transmission spectrum of port 2 exhibits periodic dips (Fig. 4b). To evaluate the performance of the interferometer, we consider a critical parameter called the extinction ratio (ER), defined as the ratio of the transmittance at the dip wavelength to that at the nearest peak wavelength. Figure 4c presents the experimental results of the ER as a function of wavelength. The ER is > 20 dB in the wavelength range of 1530 nm to 1583 nm (the region shaded in orange). This



indicates that the interference functionality can cover a bandwidth of 53 nm with a 20-dB ER.

Furthermore, the length difference between two waveguides can be extracted by applying Fourier transform on the transmission spectrum. After introducing the dispersion of strip waveguide, we can obtain the length difference from the peak position of Fourier transform result [see details in Supplementary Section H]. In Fig. 4d, the Fourier transformed magnitude shows a peak around 100 µm (green line), which agrees reasonably with the practical sample parameter. Notably, even in the presence of the dimensional error of $\Delta s = \pm 10$ nm, the extracted peaks remain around 100 µm (red and blue lines in Fig. 4d), confirming the robustness of our interferometer against dimensional errors. It is important to point out that the topological interferometer offers the potential for extensive functionalities. Furthermore, based on the same principle, we can also measure the distance in free space. By replacing one of the DBRs with a sample containing multiple reflection interfaces, we can reconstruct the axial image of a sample with different layers. This opens up new ways for applications in coherent imaging and analysis of complex media. Moreover, the topological interferometer enables not only the measurement of the length difference between two arms but also the sensing of physical quantities that change the refractive index, such as temperature, pressure, and material, etc. Leveraging the high extinction ratio provided by the topological coupler, our design holds promise for high-performance on-chip optical coherent tomography and temperature/pressure sensors.

Discussion

We have designed and realized a topological coupler that maintains a 3-dB splitting ratio over a broad wavelength range, even in the presence of common dimensional errors during practical fabrication processes. The underlying principle of the 3-dB splitting origins from the valley-Hall topology and mirror symmetry, which we have theoretically elucidated by deriving a wavelengthinsensitive scattering matrix. The tolerance analysis confirmed the robustness of the topological 3-dB coupler against dimensional errors, as compared to the conventional directional couplers (DCs). Furthermore, the proposed topological coupler was utilized to construct an on-chip interferometer capable of extracting the length difference between two arms. The interferometer exhibits remarkable resilience to dimensional errors, which is crucial for practical applications. This finding gives a systematic analysis on the advantages offered by topologically-protected edge modes and explicitly demonstrates the crucial performance of photonic structures. The proposal of topological splitting structure paves the way for the development of practical on-chip nanophotonic devices with topological protection. For example, the length difference measurement function can be applied in optical coherence tomographs and frequency modulated continuous wave LiDARs. To do this, the insertion loss between photonic crystals and strip waveguides should be further reduced to improve the signalnoise ratio of nanophotonic topological devices. The inverse design is anticipated to be applied for improving the performance of topological devices. In addition, the bandwidth and the footprint of topological coupler can be optimized based on the properties of topological valley edge modes [see details in Supplementary Sections G and I]. Based on VPCs, various kinds of on-chip photonic devices have been realized, such as asymmetric splitters⁵⁶, photonic switches⁵⁷ and add-drop filters⁵⁸. The design method based on topological photonic principle is demonstrated to be generalizable to many kinds of onchip devices. In consideration of the generalizability of topological-photonic-design method, the designs of topological 3-dB coupler and interferometer show promising applications for on-chip sensors, modulators, photodetectors, and wavelength division (de)multiplexers.

Materials and methods

Numerical simulation

The transmission spectra and field distributions in our devices were simulated using Ansys Lumerical FDTD software, utilizing the finite-difference time-domain (FDTD) method. The band structures and eigen modes of VPCs were calculated using the eigenmode solver of MIT Photonic Bands (MPB)⁵⁹. To ensure the accurate evaluation, 3D full-wave simulations were conducted with the same structural parameters as those used in the experiment. For the propagation simulations, perfectly matched layers (PMLs) were used at the boundaries of the simulation domains to absorb the output light and the stray light. In contrast, the band structure calculations employed periodic boundary conditions to account for the periodicity of the photonic crystal structure.

Sample fabrication

We fabricated the experimental sample on a silicon-oninsulator (SOI) wafer, with a 220 nm-thick silicon top layer and a 3μ m-thick buried oxide layer. The pattern of the devices was defined using electron-beam lithography (Vistec EBPG 5200 +). Inductively coupled plasma etching technique (SPTS DRIE-I) was employed to transfer the pattern onto the silicon layer. The strip waveguides, photonic crystals, and distributed Bragg reflectors (DBRs) were etched to a depth of 220 nm, while the grating couplers was etched to a depth of 70 nm. Finally, a silica upper-cladding layer was deposited on top of the silicon layer.

Optical characterization

For the measurements of transmission spectra and farfield images, three tunable continuous-wave lasers (Santec TSL-550/710) were utilized to cover the wavelength range from 1260 nm to 1640 nm. The incident light was launched into a fiber and then coupled to the input waveguide using a grating coupler. After passing through the devices based on VPCs, the output light was either coupled into a fiber or emitted into free space via grating couplers. To get the transmission spectra, the output light coupled to the fiber was detected by an optical power meter (Santec MPM-210). For obtaining far-field images, the output light emitted into free space was collected by a varifocal microscope objective and then imaged using an InGaAs CCD camera (Xenics Bobcat-640-GigE).

Acknowledgements

This work was supported by National Key Research and Development Program of China (Grant No. 2022YFA1404304), National Natural Science Foundation of China (Grant Nos. 62035016, 12274475, 12074443, 62105200), Guangdong Basic and Applied Basic Research Foundation (Grant Nos. 2023B1515040023, 2023B1515020072), Fundamental Research Funds for the Central Universities, Sun Yat-sen University (23lgbj021, 23ptpy01).

Data availability

The authors declare that all data supporting the findings of this study are available within the paper and its Supplementary Information files.

Conflict of interest

The authors declare no competing interests.

Supplementary information The online version contains supplementary material available at https://doi.org/10.1038/s41377-024-01512-3.

Received: 16 November 2023 Revised: 19 June 2024 Accepted: 26 June 2024

Published online: 16 July 2024

References

- Wang, C. et al. Integrated lithium niobate electro-optic modulators operating at CMOS-compatible voltages. *Nature* 562, 101–104 (2018).
- Xu, Y. L. et al. 3D-printed facet-attached microlenses for advanced photonic system assembly. *Light Adv. Manuf.* 4, 77–93 (2023).
- Kim, I. et al. Nanophotonics for light detection and ranging technology. Nat. Nanotechnol. 16, 508–524 (2021).
- Wang, J. W. et al. Integrated photonic quantum technologies. *Nat. Photonics* 14, 273–284 (2020).
- Shastri, B. J. et al. Photonics for artificial intelligence and neuromorphic computing. *Nat. Photonics* 15, 102–114 (2021).

- Xu, L. H. et al. Compact high-performance adiabatic 3-dB coupler enabled by subwavelength grating slot in the silicon-on-insulator platform. *Opt. Express* 26, 29873–29885 (2018).
- Hung, Y. J. et al. Mode-evolution-based silicon-on-insulator 3 dB coupler using fast quasiadiabatic dynamics. Opt. Lett. 44, 815–818 (2019).
- Magden, E. S. et al. Transmissive silicon photonic dichroic filters with spectrally selective waveguides. *Nat. Commun.* 9, 3009 (2018).
- Menchon-Enrich, R. et al. Light spectral filtering based on spatial adiabatic passage. Light Sci. Appl. 2, e90 (2013).
- Wang, J., He, S. L. & Dai, D. X. On-chip silicon 8-channel hybrid (de) multiplexer enabling simultaneous mode- and polarization-division-multiplexing. *Laser Photonics Rev.* 8, L18–L22 (2014).
- 11. Xu, P. P. et al. Low-loss and broadband nonvolatile phase-change directional coupler switches. *ACS Photonics* **6**, 553–557 (2019).
- Dai, D. X. et al. 10-channel mode (de)multiplexer with dual polarizations. *Laser Photonics Rev.* 12, 1700109 (2018).
- Huang, K. C. Y. et al. Electrically driven subwavelength optical nanocircuits. *Nat. Photonics* 8, 244–249 (2014).
- Halir, R. et al. Ultra-broadband nanophotonic beamsplitter using an anisotropic sub-wavelength metamaterial. *Laser Photonics Rev.* **10**, 1039–1046 (2016).
- 15. Cheben, P. et al. Subwavelength integrated photonics. *Nature* **560**, 565–572 (2018).
- Xu, Y. & Xiao, J. B. Ultracompact and high efficient silicon-based polarization splitter-rotator using a partially-etched subwavelength grating coupler. *Sci. Rep.* 6, 27949 (2016).
- 17. Shi, W. Y. et al. Rectangular dielectric metagrating for high-efficiency diffraction with large-angle deflection. *Chin. Opt. Lett.* **18**, 073601 (2020).
- 18. Ozawa, T. et al. Topological photonics. Rev. Mod. Phys. 91, 015006 (2019).
- Lu, L., Joannopoulos, J. D. & Soljačić, M. Topological photonics. Nat. Photonics 8, 821–829 (2014).
- Khanikaev, A. B. & Shvets, G. Two-dimensional topological photonics. *Nat. Photonics* 11, 763–773 (2017).
- Wu, Y. et al. Applications of topological photonics in integrated photonic devices. Adv. Optical Mater. 5, 1700357 (2017).
- Kim, M., Jacob, Z. & Rho, J. Recent advances in 2D, 3D and higher-order topological photonics. *Light Sci. Appl.* 9, 130 (2020).
- Yun, J. et al. Deep learning for topological photonics. Adv. Phys.: X 7, 2046156 (2022).
- 24. Wang, M. S. et al. Spin-orbit-locked hyperbolic polariton vortices carrying reconfigurable topological charges. *eLight* **2**, 12 (2022).
- Ha, Y. L. et al. High-fidelity mode scaling via topological-optimized on-chip metalens for compact photonic interconnection. *Light Adv. Manuf.* 4, 222–232 (2023).
- Zhang, Y. H. et al. Realization of photonic *p*-orbital higher-order topological insulators. *eLight* 3, 5 (2023).
- Wang, Z. et al. Observation of unidirectional backscattering-immune topological electromagnetic states. *Nature* 461, 772–775 (2009).
- Rechtsman, M. C. et al. Photonic Floquet topological insulators. *Nature* 496, 196–200 (2013).
- Khanikaev, A. B. et al. Photonic topological insulators. Nat. Mater. 12, 233–239 (2013).
- Dong, J. W. et al. Valley photonic crystals for control of spin and topology. *Nat. Mater.* 16, 298–302 (2017).
- 31. Barik, S. et al. A topological quantum optics interface. *Science* **359**, 666–668 (2018).
- Noh, J. et al. Observation of photonic topological valley hall edge states. *Phys. Rev. Lett.* **120**, 063902 (2018).

- He, X. T. et al. A silicon-on-insulator slab for topological valley transport. *Nat. Commun.* 10, 872 (2019).
- Shalaev, M. I. et al. Robust topologically protected transport in photonic crystals at telecommunication wavelengths. *Nat. Nanotechnol.* 14, 31–34 (2019).
- Kim, M., Kim, Y. & Rho, J. Spin-valley locked topological edge states in a staggered chiral photonic crystal. N. J. Phys. 22, 113022 (2020).
- 36. Kim, M. et al. Three-dimensional photonic topological insulator without spinorbit coupling. *Nat. Commun.* **13**, 3499 (2022).
- Peterson, C. W. et al. A quantized microwave quadrupole insulator with topologically protected corner states. *Nature* 555, 346–350 (2018).
- Mittal, S. et al. Photonic quadrupole topological phases. Nat. Photonics 13, 692–696 (2019).
- Ota, Y. et al. Photonic crystal nanocavity based on a topological corner state. Optica 6, 786–789 (2019).
- Gao, X. M. et al. Dirac-vortex topological cavities. Nat. Nanotechnol. 15, 1012–1018 (2020).
- 41. Xie, X. et al. Cavity quantum electrodynamics with second-order topological corner state. *Laser Photonics Rev.* **14**, 1900425 (2020).
- Liu, Y. et al. Bulk-disclination correspondence in topological crystalline insulators. *Nature* 589, 381–385 (2021).
- Chen, X. D. et al. Second chern crystals with inherently non-trivial topology. Natl Sci. Rev. 10, nwac289 (2023).
- Bahari, B. et al. Nonreciprocal lasing in topological cavities of arbitrary geometries. *Science* 358, 636–640 (2017).
- Bandres, M. A. et al. Topological insulator laser: experiments. Science 359, eaar4005 (2018).
- Shao, Z. K et al. A high-performance topological bulk laser based on bandinversion-induced reflection. *Nat. Nanotechnol.* 15, 67–72 (2020).
- Zeng, Y. Q. et al. Electrically pumped topological laser with valley edge modes. Nature 578, 246–250 (2020).
- Zhong, H. et al. Topological valley Hall edge state lasing. *Laser Photonics Rev.* 14, 200001 (2020).
- Mao, X. R. et al. Magic-angle lasers in nanostructured moiré superlattice. *Nat. Nanotechnol.* 16, 1099–1105 (2021).
- Yang, L. C. et al. Topological-cavity surface-emitting laser. Nat. Photonics 16, 279–283 (2022).
- Xue, H. R., Yang, Y. H. & Zhang, B. L. Topological valley photonics: physics and device applications. *Adv. Photonics Res.* 2, 2100013 (2021).
- Rosiek, C. A. et al. Observation of strong backscattering in valley-Hall photonic topological interface modes. *Nat. Photonics* 17, 386–392 (2023).
- Chen, Y. et al. Topologically protected valley-dependent quantum photonic circuits. *Phys. Rev. Lett.* **126**, 230503 (2021).
- Zhang, F. R. et al. Experimental realization of topologically-protected all-optical ILogic gates based on silicon photonic crystal slabs. *Laser Photonics Rev.* 17, 2200329 (2023).
- He, X. T. et al. Dual-polarization two-dimensional valley photonic crystals. Sci. China Phys. Mech. Astron. 65, 284212 (2022).
- 56. Wang, H. W. et al. Asymmetric topological valley edge states on silicon-oninsulator platform. *Laser Photonics Rev.* **16**, 2100631 (2022).
- Wang, H. W. et al. Ultracompact topological photonic switch based on valleyvortex-enhanced high-efficiency phase shift. *Light Sci. Appl.* **11**, 292 (2022).
- Mehrabad, M. J. et al. Chiral topological add-drop filter for integrated quantum photonic circuits. *Optica* 10, 415–421 (2023).
- Johnson, S. G. & Joannopoulos, J. D. Block-iterative frequency-domain methods for maxwell's equations in a planewave basis. *Opt. Express* 8, 173–190 (2001).